

LING5702: Lecture Notes 17

Quantifier Scope

The last step in obtaining complex ideas from sounds and gestures is quantifier scope.

Contents

17.1 Simple scope disambiguation [Schuler & Wheeler, 2014]	1
17.2 Evidence for explicit scoping [Dotlačil & Brasoveanu, 2015]	2

17.1 Simple scope disambiguation [Schuler & Wheeler, 2014]

We'll assume the following constants (with a localist representation: referential states are δ_v):

1. $V \in \mathbb{R}$: a maximum number of referential states (variables in lambda calculus expressions);
2. $\mathbf{q} \in \{0, 1\}^V$: a vector of zeros or ones indicating if each referential state is a quantification;
3. $\mathbf{v} \in \mathbb{R}^V$: a vector of precedence ('readiness') values for each referential state, based on:
 - (a) quantifier type (e.g. **Each** has low precedence, so it usually scopes last/highest)
 - (b) participated-in predicates (e.g. y in **ln** $x y$ will scope higher than x)
 - (c) order in sentence (this enforces a preference for in-situ scope)
4. $\mathbf{E}_n \in \mathbb{R}^{V \times V}$: a matrix of associations from functions to arguments numbered by n ;

We'll also assume **inheritance** associations ('rin') from the lecture notes on sentence processing:

$$\mathbf{E}_{\text{rin}} = \mathbf{E}_1 \text{diag}(\mathbf{q}) \mathbf{E}_2^\top$$

We'll need **closure** matrices directly associating states connected by any number of associations:

$$\mathbf{E}_P = \mathbf{I} + \sum_{n=1}^N \prod_{i=1}^n \sum_{\ell \in \{1,2,3,\dots\}} \mathbf{E}_\ell \text{diag}(\mathbf{1}-\mathbf{q}) + \text{diag}(\mathbf{1}-\mathbf{q}) \mathbf{E}_\ell^\top$$

$$\mathbf{E}_I = \mathbf{I} + \sum_{n=1}^N \prod_{i=1}^n \sum_{\ell \in \{\text{cin}, \text{ein}, \text{rin}\}} \mathbf{E}_\ell + \mathbf{E}_\ell^\top$$

First, initialize iteration-dependent variables:

1. $\mathbf{Q}_0 = \mathbf{0}^{V \times V}$: an initially empty matrix of immediate outscopings;
2. $\mathbf{P}_0 = \mathbf{E}_P + \mathbf{I} - \text{diag}(\mathbf{E}_P)$: a matrix of fully-connected partitions, starting with no inheritances;
3. $\mathbf{u}_0 = \sum_{v \text{ s.t. } v = \text{argmax} \text{diag}(\mathbf{v}) \mathbf{P}_0 \delta_v} \delta_v$: a vector of used referential states, starting with the readiest.

Then, for each iteration $i \in \{1, 2, 3, \dots\}$ such that some states remain un-used ($\mathbf{u}_{i-1} \neq \mathbf{1}$):

1. $u_i = \operatorname{argmax} \operatorname{diag}(\mathbf{v}) \underbrace{\operatorname{diag}(\mathbf{1} - \mathbf{E}_I (\mathbf{1} - \mathbf{u}_{i-1}))}_{\text{not connected to unused}} (\mathbf{1} - \mathbf{Q}_{i-1}^\top \mathbf{1})$: get readiest used un-scoped state;
2. $\mathbf{P}_i = \mathbf{a} \mathbf{a}^\top + \underbrace{\mathbf{P}_{i-1} \operatorname{diag}(\mathbf{1} - \mathbf{a})}_{\text{copy non-merged partitions}}$ where $\mathbf{a} = \mathbf{P}_{i-1} \mathbf{E}_I \delta_{u_i}$: merge partitions connected via u_i ;
3. $v_i = \operatorname{argmax} \operatorname{diag}(\mathbf{v}) \operatorname{diag}(\mathbf{1} - \mathbf{u}_{i-1}) \mathbf{P}_i \delta_{u_i}$: find readiest unused state in new partition;
4. $\mathbf{Q}_i = \mathbf{Q}_{i-1} + \delta_{v_i} \delta_{u_i}^\top \mathbf{E}_I$: associate referential states in scope matrix;
5. $\mathbf{u}_i = \mathbf{u}_{i-1} + \delta_{v_i}$: add v_i as used.

Participant and scope associations define lambda calculus expressions as described earlier.

17.2 Evidence for explicit scoping [Dotlačil & Brasoveanu, 2015]

It does seem that scope is explicitly calculated like this (i.e. doesn't remain underspecified):

- **stimuli:** sentences presented in eye-tracking:
 - (a) *A caregiver comforted a child every night. The caregivers wanted the children to...*
 - (b) *A caregiver comforted a child every night. The caregivers wanted the child to...*
 - (c) *A caregiver comforted a child every night. The caregiver wanted the children to...*
 - (d) *A caregiver comforted a child every night. The caregiver wanted the child to...*

These analyses are eliminated at *caregiver*, but neither is the preferred in-situ analysis:

<p>All (λ_t Night t) (λ_t Some (λ_k Caregiver k) (λ_k Some (λ_c Child c) (λ_c Comfort $t k c$)))</p>	<p>Some (λ_c Child c) (λ_c All (λ_t Night t) (λ_t Some (λ_k Caregiver k) (λ_k Comfort $t k c$)))</p>
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The preferred in-situ (first) analysis is eliminated at *children*:

<p>Some (λ_k Caregiver k) (λ_k Some (λ_c Child c) (λ_c All (λ_t Night t) (λ_t Comfort $t k c$)))</p>	<p>Some (λ_k Caregiver k) (λ_k All (λ_t Night t) (λ_t Some (λ_c Child c) (λ_c Comfort $t k c$)))</p>
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- **measure:** eye-tracking fixation durations at *children* (and spillover word).
- **results:** singular-plural (c) is slowest at *children*, suggests dynamic reanalysis there.

(We don't have a scope re-analysis model, though.)

References

- [Dotlačil & Brasoveanu, 2015] Dotlačil, J. & Brasoveanu, A. (2015). The manner and time course of updating quantifier scope representations in discourse. *Language, Cognition and Neuroscience*, 30(3), 305–323.
- [Schuler & Wheeler, 2014] Schuler, W. & Wheeler, A. (2014). Cognitive compositional semantics using continuation dependencies. In *Third Joint Conference on Lexical and Computational Semantics (*SEM'14)*.